



Introduction to Random Signals and Applied Kalman Filtering

With Matlab Exercises and Solutions, Third Edition
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